# The Crystal Structure of the High Temperature Form of $\mathbf{T a}_{2} \mathbf{O}_{5}$ 

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#### Abstract

The structure of the high temperature form of $\mathrm{Ta}_{2} \mathrm{O}_{5}$ can be stabilized by doping with 2 mole $\% \mathrm{Sc}_{2} \mathrm{O}_{3}$ and single crystals have been prepared from a $\mathrm{Ta}_{2} \mathrm{O}_{5}-\mathrm{Sc}_{2} \mathrm{O}_{3}(98: 2)$ composition by the Czochralski technique. The crystal system which at first appeared to be body-centered tetragonal has been determined to be face-centered monoclinic, space group $C 2$ with $a=35.966 \AA, b=3.810 \AA, c=3.810 \AA, \beta=96^{\circ} 7^{\prime}$. Least-squares refinement cycles reduced the reliability index $R$ to 0.089 .

The structure consists of $\alpha \mathrm{UO}_{3}$-type blocks in which each tantalum atom is surrounded by a pentagonal bipyramid of oxygen atoms. These blocks are infinite in two directions and are separated from similar blocks along a third direction by shear planes. In the vicinity of these shear planes the tantalum atoms are surrounded by distorted octahedral coordination polyhedra. It is believed that the stabilizing effect of the $\mathrm{Sc}_{2} \mathrm{O}_{3}$ impurity is due to an increase in the concentration of shear planes. Random shear planes (Wadsley defects) are introduced at approximately $300 \AA$ intervals along the large axis by doping with a substance $\left(\mathrm{Sc}_{2} \mathrm{O}_{3}\right)$ which has cations ( Sc ) large enough to substitute for the host ( Ta ) but a lower oxygen:metal ratio than the host compound $\left(\mathrm{Ta}_{2} \mathrm{O}_{5}\right)$.


## Introduction

$\mathrm{Ta}_{2} \mathrm{O}_{5}$ was first reported to undergo a transformation to a high temperature form by Lagergren and Magneli (1). Reisman, Holtzberg, et al. (2) reported the phase transition to occur at $1360^{\circ} \mathrm{C}$ and indicated that the high temperature polymorph probably had triclinic symmetry when quenched to room temperature. Laves and Petter (3) and Waring and Roth (4) have shown that this form actually undergoes several unquenchable phase transitions upon cooling from high temperatures. For this reason good single crystals of the high temperature form of $\mathrm{Ta}_{2} \mathrm{O}_{5}\left(H-\mathrm{Ta}_{2} \mathrm{O}_{5}\right)$ can not be grown from pure material and examined at room temperature. However, Roth, Waring, and Brower (5) have shown that several impurity ions when added to $\mathrm{Ta}_{2} \mathrm{O}_{5}$ in small amounts enable the apparently tetragonal form of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ to be obtained at room temperature by quenching from above $\sim 1400^{\circ} \mathrm{C}$. Furthermore it was demonstrated that large single crystals of this apparently tetragonal $H-\mathrm{Ta}_{2} \mathrm{O}_{5}$ could be grown by the Czochralski technique utilizing an iridium crucible and about $2-4 \mathrm{~mole} \% \mathrm{Sc}_{2} \mathrm{O}_{3}$ as the "stabilizing" impurity ion.

[^0]A small, annealed, cleavage fragment of one of these crystals has been used in the present study.

As no reasonably good quality crystals of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ have been prepared previously there have not been any prior published attempts to determine the structure. However, Laves, Moser, and Petter (6) have pointed out that the structure of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ should probably be similar to that of $\eta$ (eta) or $P-\mathrm{Nb}_{2} \mathrm{O}_{5}$. This similarity has been pointed out by Andersson (7) and also by Holtzberg (private communication, Sept. 27, 1968). To a first approximation then, $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ has been considered to be made up of a series of edge and corner shared octahedra with six molecules in the unit cell instead of the four molecules found in $\eta(P)-\mathrm{Nb}_{2} \mathrm{O}_{\mathrm{s}}$.

## Experimental

Powder photographs of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ stabilized by 2 mole $\% \mathrm{Sc}_{2} \mathrm{O}_{3}$ can be completely indexed on the basis of a tctragonal unit-cell with dimensions $a=3.810$ and $c=35.764 \AA$. Single-crystal Weissenberg photographs collected with copper radiation, suggested the Laue symmetry $4 / \mathrm{mmm}$ and small deviations from this symmetry were initially attributed to absorption effects ( $\mu=1146 \mathrm{~cm}^{-1}$ for

TABLE I
Crystal Dimensions

| $h k l^{a}$ | $D^{b}$ | $h k l^{a}$ | $D^{b}$ |
| :--- | :--- | :--- | :--- |
| 209 | 0.010 | $10 \overline{2} \overline{0}$ | 0.025 |
| $\overline{2} 0 \overline{9}$ | 0.101 | 010 | 0.044 |
| 1020 | 0.025 | $0 \overline{1} 0$ | 0.044 |

[^1]$\mathrm{CuK} \propto$ radiation). Systematic absences in spectra indicated the space group $14_{1} /$ amd .

For data collection, a single crystal fragment, transparent and roughly tabular in shape ( $0.02 \times$ $0.05 \times 0.09 \mathrm{~mm}$ ) was mounted about the $b$ axis on a single crystal orienter. Intensities were measured by the $2 \theta$ scan method with $\mathrm{Mo} K_{\alpha}$ radiation. The rate of scanning was $1^{\circ} / \mathrm{min}$, and the scan range (SR) was calculated using the equation $\mathrm{SR}=$ $2.40+1.0 \tan \theta$. The backgrounds were measured for 60 sec at $2 \theta \pm \frac{1}{2} \mathrm{SR}$. The intensities of three standard reflections were checked periodically during the run to monitor diffractometer and crystal stability. No significant changes were observed in these standards. Data were collected out to $60^{\circ}$ in $2 \theta$ and one-half of the reciprocal lattice was measured. Counting statistics were used to calculate a standard deviation ( $\sigma$ ) for each intensity and if the net number of counts was less than $2 \sigma$ the reflection was considered as a "less than" and its intensity was set equal to $2 \sigma$.
The resulting intensities were corrected for Lorentz, polarization and absorption effects ( $\mu=$ $666 \mathrm{~cm}^{-1}$ for $\mathrm{Mo} K_{\alpha}$ radiation). For the latter calculation the crystal measurements listed in Table I were used together with the DATAP program of Coppens, Leiserowitz, and Rabinovich (8) to calculate absorption corrections at 125 Gaussian grid points.

The atomic scattering factors for $\mathrm{O}^{2-}$ and $\mathrm{Ta}^{5+}$ were taken from Suzuki (9) and Cromer and Waber (10), respectively, and the real part of the anomalous
dispersion correction was applied to the scattering curve for tantalum [Dauben and Templeton, (11)]. No allowance was made for the scandium content.

## Determination of the Structure

The space group $I 4_{1} /$ amd has equivalent positions that are multiples of 4 . The twelve tantalum atoms in the unit-cell can therefore be placed in special positions $4 a$ or $4 b$ and in special positions $8 c, 8 d$ or $8 e$. However, the 30 oxygen atoms (actually 29.76 due to the $\mathrm{Sc}_{2} \mathrm{O}_{3}$ impurity) cannot be accommodated using the $4-, 8$-, 16 - and 32 -fold equivalent positions unless some positions are fractionally occupied. It seemed probable that the tantalum atoms are indeed distributed in a manner similar to that described above, but the oxygen atoms have a less symmetrical distribution than that required by the space group $I 4_{1} / a m d$. In this case, and also because of the short $a$ and $b$ unit-cell dimensions, a reasonable approach to the structure determination is to initiate a solution in projection using the less extensive plane group symmetries rather than the very large number of space groups that must be considered as alternatives to $I 4_{1} /$ amd .

The systematic spectral absences based upon the largest amount of data are those with $h+k+$ $l \neq 2 \mathrm{n}$. It seemed likely therefore that both (100) and (010) projections would be face-centered. Provided that both of these projections have rectangular symmetry then the plane groups of either projection must be Cm or Cmm .

The (hol) Patterson projection is shown in Fig. 1. Tantalum atoms placed in positions $4 a$ and $8 e$ (with $Z=0.042$ ) of space group $I 4_{1} /$ amd provided a satisfactory starting model (Fig. 2a). The plane group corresponding to this atomic arrangement is Cmm with atoms in positions $4 e$. Least-squares refinement cycles failed to bring the residual $R$ to below 0.30 and symmetry restrictions were therefore relaxed so as to allow the $x$ coordinate of the metal atoms to vary. This resulted in an appreciable decrease in $R$ (to 0.14 ) and the correct plane group appeared to be $C m$ with metal atoms in positions $4 b$.

A difference Fourier synthesis clearly showed oxygen atoms in general fourfold positions $4 b$ and


Fig. 1. The hol Patterson function, contoured at arbitrary levels.


Fig. 2. (a) A trial model in the space group $I 4_{1} / a m d$ showing tantalum atoms in positions $4 a$ and $8 e$ (with $z=0.042$ ). Like motifs are related by symmetry elements. Dark motifs represent atoms with $y=\frac{1}{2}$ and clear motifs represent atoms at $y=0$. The plane group symmetry of the projection is Cmm. (b) Some symmetry elements of $I 4_{1} / a m d$ can be relaxed to give the space groups Cc. The metal atom positions shown in Fig. 2(a) can change slightly but those atoms related across the glide plane at $z=\ddagger$ have the same $y$ coordinate. The unit-cell shown here is the same as that selected for the tetragonal system and the space group depicted above is therefore $I c$. (c) The space group $C 2$ utilizes some of the symmetry elements of $I 4_{1} / a m d$ and these are shown above. Choosing the same orthogonal unit-cell as above, the space group is $I 2$ and the atoms either side of the screw axis at $z=\frac{1}{4}$ do not have the same $y$ coordinate. (d) The orientation of the correct monoclinic unit-cell of $H-\mathrm{Ta}_{2} \mathrm{O}_{5}$ with respect to the orthogonal unit-cell chosen on the basis of space group $I 4_{1} / \mathrm{amd}$.

| Orthogonal cell | Monoclinic cell |
| :--- | :--- |
| $a_{1}=3.810 \AA$ | $a_{2}=35.966 \AA$ |
| $b_{2}=3.810 \AA$ | $b_{2}=3.810 \AA$ |
| $c_{1}=35.764 \AA$ | $c_{2}=3.810 \AA$ |
| Space group $I 4_{1} /$ amd | $\beta=96^{\circ} 7^{\prime}$ |
|  | Space group $C 2$ |

one set in the twofold position $2 a$, making a total of 30 in the unit-cell. This correct number of oxygen atoms together with acceptable bond distances and coordination polyhedra, shown in Fig. 3, left no doubt that the model was correct and refinement proceeded smoothly to yield a value of $R(h o l)$ of 0.086 .

The same procedure was tried with the okl data. The metal atoms are known to be situated in positions closely related to $4 a$ and $8 e$ (with $Z \approx 0.042$ ) of space group $I 4_{1} /$ amd (see Fig. 2a). The (100) projection of this space group also has Cmm symmetry but the ( 001 ) mirror plane is moved $C / 4$ with respect to the position of the equivalent mirror plane in the (100) projection. Attempted
refinement of metal atom coordinates in the plane group Cmm was not successful but, as before, an acceptably low $R$ value of 0.13 was obtained by allowing both positional parameters of each atom to vary and refining in the plane group Cm . Subsequent difference Fourier synthesis, however, failed to show well-formed oxygen peaks either in the correct numbers or which correlated with peaks found for oxygen atoms in the ( 010 ) projection.

A reassessment of the situation showed that if the plane groups of the (100) and (010) projections were each $C m$ then the space group for the structure will be $C c$ with the unique axis parallel to $c$ (Fig. 2b). In this case oxygen atoms $O(6)$, shown in projection in Fig. 3 with $z$ coordinates of approximately 0.25 ,


Fig. 3. An (010) projection of the structure of $H-\mathrm{Ta}_{2} \mathrm{O}_{5}$. Heavily shaded polyhedra are located at $y=\frac{1}{2}$ and the remainder are at $y=0$.
would have identical coordinates ( $y$ ) parallel to the projection axis resulting in a close approach between these atoms. The structure of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$, as inferred from the ( 010 ) projection and known spacial distribution of metal atoms, can be regarded as $\mathrm{UO}_{3}$-type blocks of Ta O polyhedra connected to each other by shear planes. In the $\mathrm{UO}_{3}$ structure [Zachariasen (12)], the six oxygen atoms forming the equatorial plane of the hexagonal bipyramidal polyhedra are puckered. A similar arrangement in $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ would mean that the oxygen atoms $\mathrm{O}(6)$, referred to above, would not have the same $y$ coordinates but rather they would be located at $y$ and $\bar{y}$. In this case the glide planes shown in Fig. 2(b) would be replaced by twofold rotation and screw axes, shown in Fig. 2c. The space group becomes $C 2$ and the plane group of the projection along the unique axis would be $P 2$ rather than Cm , as before.

Refinement of the $y$ and $z$ metal atom coordinates was thercfore carricd out in the plane group $P 2$ and the resulting difference Fourier synthesis clearly showed the correct number of oxygen atoms in positions which correlated with those obtained from the (010) projection. Least-squares refinement cycles reduced $R$ to 0.09 .

It was now possible to refine the structural atomic parameters using full three-dimensional data. For correctness the data should be reindexed on the basis of the monoclinic cell whose direct-lattice unit-cell vectors are related to those of the orthogonal cell (defined above) by the transformation matrix.
othog (1)


This was not done because it was more convenient to refer to the structure in terms of the orthogonal unit-cell that has previously been reported for it [Waring and Roth (4)]. The asymmetric quarter of the reciprocal lattice was therefore chosen on the basis of the orientation of the symmetry elements of the space group $I 2$ and the programs of Stewart (13) were used for the subsequent refinement cycles.

It is doubtful whether a systematic examination of the reciprocal lattice involving a point by point comparison would have revealed the monoclinic symmetry of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$. Deviations from tetragonal symmetry are extremely small since the heavy tantalum atoms have essentially a tetragonal distribution. The trial and error method described above makes use of the combined effect of a large number of data and, when used with caution, this approach can be useful in determining the true symmetry, and therefore structure, of a crystal.

The final atomic parameters are listed in Table II and these were used to calculate the final structure factors. ${ }^{1}$ The final $R$ value for all observed data is 0.089 , and the weighted $R$ value is 0.078 .

## Description of the Structure

Tantalum atoms $M(3)$ are each surrounded by seven oxygen atoms in the form of a distorted pentagonal bipyramid. Tantalum-oxygen bond distances vary between $1.85(7)$ and $2.38(4) \AA$ (see Table III) and average at $2.04 \AA$. The $M(3)$ poly-

[^2]TABLE II
Final Positional and Thermal Parameters for $\boldsymbol{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}{ }^{a}$
Other atoms in the orthogonal unit-cell are related to those listed below by the symmetry elements of the space group I2. Numbers in parenthesis are estimated standard deviations in the least significant digits.

|  | $x / a$ |  | $y / b$ |  | $z / c$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| M(1) | 0.00500 |  | -0.00597(80) |  | $0.045682(78)$ |  |
| M(2) | -0.0022(55) |  | 0.49419(82) |  | $0.12514(10)$ |  |
| M(3) | $0.4813(29)$ |  | 0.49882(67) |  | $0.204529(77)$ |  |
| O(1) | 0.933(15) |  | $0.501(9)$ |  | $0.1809(11)$ |  |
| O(2) | 0.969(27) |  | 0.488(10) |  | $0.0712(11)$ |  |
| $\mathrm{O}(3)$ | 0.429(15) |  | 0.492(10) |  | $0.1383(10)$ |  |
| O(4) | 0.544(16) |  | -0.007(10) |  | $0.0526(11)$ |  |
| $\mathrm{O}(5)$ | 0.458(32) |  | -0.006(13) |  | $0.1964(14)$ |  |
| $\mathrm{O}(6)$ | 0.146(19) |  | 0.487(16) |  | 0.2420(14) |  |
| O(7) | $0.136(24)$ |  | 0.250 |  | 0.0000 |  |
| $\mathrm{O}(8)$ | $0.005(46)$ |  | 0.996(11) |  | 0.1122(12) |  |
|  | ${ }^{\text {b }} \beta(11) \times 10^{4}$ | $\beta(22) \times 10^{4}$ | $\beta(33) \times 10^{5}$ | $\beta(12) \times 10^{4}$ | $\beta(13) \times 10^{5}$ | $\beta(23) \times 10^{5}$ |
| M(1) | 189(28) | 233(17) | 10(2) | 53(46) | -56(40) | 28(15) |
| M(2) | 318(25) | 159(15) | 11(2) | -1(44) | -109(40) | 33(11) |
| M(3) | 343(33) | 28(13) | 12(3) | 46(42) | -165(40) | 30(14) |
| $\mathrm{O}(1)$ | .25(68) ${ }^{\text {c }}$ |  |  |  |  |  |
| $\mathrm{O}(2)$ | .77(96) |  |  |  |  |  |
| O(3) | .09(90) |  |  |  |  |  |
| O(4) | .39(72) |  |  |  |  |  |
| O(5) | 2.17(1.64) |  |  |  |  |  |
| O(6) | 1.42(1.22) |  |  |  |  |  |
| O(7) | 1.01(1.60) |  |  |  |  |  |
| $\mathrm{O}(8)$ | 1.39(1.32) |  |  |  |  |  |

[^3]$$
\exp \left\{-\left[\beta_{11} h^{2}+\beta_{22} k^{2}+\beta_{33} l^{2}+2 \beta_{12} h k+2 \beta_{13} h l+2 \beta_{23} k l\right]\right\}
$$
${ }^{c}$ The values are $B\left(\AA^{2}\right)$.
hedra share corners with each other and form a sheet two polyhedra wide, which extends infinitely along the $a$ and $b$ directions. The structure within this sheet is very similar to that of $\mathrm{UO}_{3}$ [Zachariasen, (12)].

Tantalum atoms $M(1)$ and $M(2)$ are each surrounded by six oxygen atoms in the form of a distorted octahedron. Each $M(2)$ octahedron shares an edge with an adjacent $M(3)$ pentagonal bipyramid, two edges with $M(1)$ octahedra and is joined with four $M(2)$ octahedra by corner sharing. Each $M(1)$ octahedron shares two edges with $M(2)$ polyhedra and is joined with five other $M(1)$ octahedra by corner sharing. Bond distances for these octahedra are listed in Table III.

## Discussion

The crystal structure of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ can thus be viewed as either a modification of the $\alpha \mathrm{UO}_{3}$ type structure with shear planes to accommodate the difference in cation/anion ratio, or as a combination of $\alpha \mathrm{UO}_{3}$ blocks with $\eta(P)-\mathrm{Nb}_{2} \mathrm{O}_{5}$ blocks. The crystal structure of eta- $\mathrm{Nb}_{2} \mathrm{O}_{5}$ after Petter and Laves (14), is shown in Fig. 4. This structure shows an alternating sequence of four octahedra at zero and one-half for both hOl and Okl projections. The arrangement of octahedra which can be postulated to account for a unit cell with six molecules and a $c$ axis of approximately the length found in $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ is shown in Fig. 5. However, this postulated structure

## TABLE III

Interatomic Distances (Å) Within Each Coordination Polyhedron ${ }^{a}$

| $\mathrm{M}(1) \mathrm{Octahedron}$ |  |
| :---: | :--- |
| $\mathrm{M}(1)-\mathrm{O}(4)^{1}$ | $1.774(63)$ |
| $\mathrm{O}(4)$ | $2.068(63)$ |
| $\mathrm{O}(7)$ | $1.967(24)$ |
| $\mathrm{O}(8)^{2}$ | $2.380(42)$ |
| $\mathrm{O}(2)^{1}$ | $2.096(40)$ |
| $\mathrm{O}(2)^{3}$ | $2.138(39)$ |
| $\mathrm{O}(4)-\mathrm{O}(7)^{1}$ | $2.63(7)$ |
| $\mathrm{O}(7)^{1}-\mathrm{O}(4)^{1}$ | $3.09(8)$ |
| $\mathrm{O}(4)^{1}-\mathrm{O}(8)^{2}$ | $2.76(10)$ |
| $\mathrm{O}(8)^{2}-\mathrm{O}(4)$ | $2.96(13)$ |
| $\mathrm{O}(2)^{1}-\mathrm{O}(7)^{1}$ | $2.78(5)$ |
| $\mathrm{O}(4)^{1}$ | $2.58(9)$ |
| $\mathrm{O}(8)^{2}$ | $2.43(6)$ |
| $\mathrm{O}(4)$ | $2.97(10)$ |
| $\mathrm{O}(2)^{3}-\mathrm{O}(7)^{1}$ | $3.91(9)$ |
| $\mathrm{O}(4)^{1}$ | $2.62(8)$ |
| $\mathrm{O}(8)^{2}$ | $2.43(6)$ |
| $\mathrm{O}(4)$ | $2.99(10)$ |

M(3) Pentagonal
Bipyramid
M(3)-O(5) $1.948(50)$
$O(5)^{6} \quad 1.910(52)$
$\mathrm{O}(1) \quad 1.917(53)$
$O(3) \quad 2.377(39)$
$O(1)^{1} \quad 2.254(57)$
$\mathrm{O}(6) \quad 1.853(66)$
$\mathrm{O}(6)^{4} \quad 2.011(58)$
$\mathrm{O}(6)^{5} \quad 2.866(65)$
$\mathrm{O}(1)-\mathrm{O}(3) \quad 2.45(8)$
$\mathrm{O}(3)-\mathrm{O}(1)^{1} \quad 2.43(8)$
$\mathrm{O}(1)^{1}-\mathrm{O}(6) \quad 2.33(7)$
$\mathrm{O}(6)-\mathrm{O}(6)^{4} \quad 2.02(14)$
$\mathrm{O}(6)^{4}-\mathrm{O}(1) \quad 2.96(10)$
$O(5)-O(1) \quad 2.70(10)$
$\mathrm{O}(3) \quad 2.82(7)$
$\mathrm{O}(1)^{1} \quad 2.84(10)$
$\mathrm{O}(6) \quad 2.76(9)$
$\mathrm{O}(6)^{4} \quad 3.04(10)$
$\mathrm{O}(5)^{6}-\mathrm{O}(1) \quad 2.66(9)$
$\mathrm{O}(3) \quad 2.82(11)$
$\mathrm{O}(1)^{1} \quad 2.80(10)$
$\mathrm{O}(6) \quad 2.79(8)$
$\mathrm{O}(6)^{4} \quad 2.95(10)$

| $\mathrm{M}(2)$ Octahedron |  |
| :---: | :--- |
| $\mathrm{M}(2)-\mathrm{O}(8)$ | $1.968(42)$ |
| $\mathrm{O}(8)^{2}$ | $1.952(42)$ |
| $\mathrm{O}(2)^{1}$ | $1.932(42)$ |
| $\mathrm{O}(3)^{1}$ | $2.217(59)$ |
| $\mathrm{O}(1)^{1}$ | $2.009(39)$ |
| $\mathrm{O}(3)$ | $1.709(59)$ |
| $\mathrm{O}(3)-\mathrm{O}(2)^{1}$ | $2.97(8)$ |
| $\mathrm{O}(2)^{1}-\mathrm{O}(3)^{1}$ | $3.16(9)$ |
| $\mathrm{O}(3)^{1}-\mathrm{O}(1)^{1}$ | $2.45(8)$ |
| $\mathrm{O}(1)^{1}-\mathrm{O}(3)$ | $2.43(8)$ |
| $\mathrm{O}(8)-\mathrm{O}(2)^{1}$ | $2.43(6)$ |
| $\mathrm{O}(3)^{1}$ | $3.06(12)$ |
| $\mathrm{O}(1)^{1}$ | $3.11(6)$ |
| $\mathrm{O}(3)$ | $2.68(10)$ |
| $\mathrm{O}(8)^{2}-\mathrm{O}(2)^{1}$ | $2.38(8)$ |
| $\mathrm{O}(3)^{1}$ | $3.04(7)$ |
| $\mathrm{O}(1)^{1}$ | $3.13(9)$ |
| $\mathrm{O}(3)$ | $2.66(11)$ |



Fig. 4. The crystal structure of $\eta(P)-\mathrm{Nb}_{2} \mathrm{O}_{5}$, after Petter and Laves ( 6 ).
contains alternating units of six octahedra only in the $h O l$ projection; the $O k l$ projection shows a sequence of $4-2-4-2$. The unit cell is actually facecentered rather than body-centered and the Patterson projections would be quite different for the two projections. Furthermore, the Patterson projection, shown in Fig. 1, for $H-\mathrm{Ta}_{2} \mathrm{O}_{5}$ does not allow an interpretation of six-metal atoms occurring at the same level.

The unit-cell can be forced into a body-centered configuration if the oxygen atom in the twofold site is moved by $1 / 4$ of the $3.8 \AA$ cell edge as shown in Fig. 6. This type of movement has been labelled " $1 / 4$ shear" but this nomenclature should not be confused with the term "crystallographic shear" used to describe a change from corner-sharing to


Fig. 5. Hypothetical structure of a phase with six molecules ( $\mathrm{B}_{12} \mathrm{O}_{30}$ ) with a unit-cell approximately that of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$, but face-centered.


Fig. 6. Hypothetical structure of a phase similar to that of Fig. 5 but with " $\frac{1}{4}$ shear" to form body-centered cell.
edge-sharing of octahedra. Although the new unitcell shown in Fig. 6 is body-centered the $O \mathrm{kl}$ projection has six octahedra at each level of the cell while the $h O l$ projection has a sequence of 4-1-1-4-1-1. Therefore this structure is still inconsistent with the Patterson projection.

An alternate method to account for the unit cell with six molecules is to intermix units of octahedra and hexagonal bipyramids. Such an arrangement is shown in Fig. 7 with both the octahedra and hexagonal bipyramids drawn as ideal polyhedra for simplicity of construction. This postulated structure consists of a configuration of metal atoms in a 4-1-1-4-1-1 sequence for the Okl projection and 4-2-4-2 for the hOl projection. However,


Fig. 7. Hypothetical structure of a phase with approximately the same dimensions as Fig. 5 but containing $\frac{1}{3}$ of the metals in hexagonal bipyramidal coordination.


Fig. 8. Ideal structure of $H-\mathrm{Ta}_{2} \mathrm{O}_{5}$, similar to Fig. 7 but with " $\frac{1}{4}$ shear" to form body-centered cell.
the unit-cell is face-centered rather than bodycentered. The ideal body-centered cell consistent with the Patterson projection of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ can be formulated and is illustrated in Fig. 8 by combining the $1 / 4$-shear feature of Fig. 6 with the mixed octahedra-hexagonal bipyramid scheme of Fig. 7.

An $O k l$ projection of the $H-\mathrm{Ta}_{2} \mathrm{O}_{5}$ structure, obtained from the two dimensional refinement of the $O k l$ data only (Fig. 9) illustrates the fact that the space occupied by the hexagonal bipyramids is actually little greater than that occupied by the octahedra. No attempt has been made in this figure to illustrate that the hexagonal bipyramid is actually distorted into a pentagonal bipyramid as shown in Fig. 3.

In Fig. 10 an infinite array of such hexagonal bipyramids is shown having a total composition of $\mathrm{B}_{2} \mathrm{O}_{6}\left(\mathrm{~B}=\right.$ metal ion) (as in $\alpha \mathrm{UO}_{3}$ ). A local reduction in oxygen content can be obtained through


Fig. 9. An $O k l$ projection of the $H-\mathrm{Ta}_{2} \mathrm{O}_{5}$ structure, obtained from the two-dimensional refinement of the Okl data only.

octahedra and consequent reduction in oxygen content.
"crystallographic shear" in a plane perpendicular to the figure, as illustrated in Fig. 10b. This crystallographic shear results in two edge-shared octahedra in place of two previously edge-shared hexagonal bipyramids (or corner-shared pentagonal bipyramids). The two metal atoms which were formerly on the same level in the $b$ direction and displaced by half the unit cell in $a$ are now on the same level in the $a$ direction and displaced by half the unit cell in $b$.

Figure $11(\mathrm{a})$ shows that the phase with the stoichiometry of $\mathrm{B}_{12} \mathrm{O}_{30}\left(H-\mathrm{Ta}_{2} \mathrm{O}_{5}\right)$ actually contains four such shear planes per unit-cell and that the octahedra in the structure of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ can be considered to be the result of crystallographic shear of an $\alpha \mathrm{UO}_{3}$ type structure. If such shear is carried to a maximum, the end result [Fig. 11(b)] is a hypothetical phase with a $c$ axis of approximately one-half that of $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ and a stoichiometry of $\mathrm{B}_{12} \mathrm{O}_{26}$.
It is postulated that the $\mathrm{Sc}_{2} \mathrm{O}_{3}$ used to stabilize the $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ crystal structure is accommodated by a replacement of some $\mathrm{Ta}^{5+}$ ions by $\mathrm{Sc}^{3+}$ and a local reduction in oxygen content by a random shear mechanism similar to that illustrated in Fig. 10(b). Such a random shear has been termed "Wadsley shear" by Andersson (15) and this is probably the mechanism which accounts for the solid solutions reported in $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ [Waring and Roth, (4); Roth, Waring, and Brower, (5)]. As no superstructure lines have ever been found in $x$-ray

Fig. 11. "Crystallographic-shear" in the $H-\mathrm{Ta}_{2} \mathrm{O}_{5}$ structure. (a) $\mathrm{B}_{12} \mathrm{O}_{30}$; (b) $\mathrm{B}_{12} \mathrm{O}_{26}$.
patterns of such solid solutions it must be concluded that the shear mechanism is truly random and that these materials are really Wadsley-shear-type nonstoichiometric solid solutions. As each such shear results in a reduction of two oxygen ions per unit-cell a composition of $\mathrm{Ta}_{2} \mathrm{O}_{5}: \mathrm{Sc}_{2} \mathrm{O}_{3}(98: 2)$ would contain about one shear plane every eight unit-cells and the (random) shear planes would be about $286 \AA$ apart.

An attempt to observe these Wadsley defects by the electron microscope lattice image technique (J. Allpress, private communication, 1969) has not been successful due to the very excessive damage apparently caused by mechanical shear during grinding of the specimens. A technique such as ion thinning might hopefully prove more fruitful for preparation of specimens for this lattice image examination.

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[^1]:    ${ }^{a}$ Indices of each bounding plane.
    ${ }^{n}$ Perpendicular distance in mm of each plane from an origin at the center of the crystal.

[^2]:    ${ }^{1}$ A table of observed and calculated structure amplitudes from this analysis has been deposited as Document No. NAPS-01227 with the ASIS National Auxiliary Publication Service, c/o CCM Information Corp., 909 3rd Ave., New York, N.Y. 10002. A copy may be secured by citing the document number and by remitting $\$ 5.00$ for photocopies or $\$ 2.00$ for microfiche. Advance payment is required. Make checks or money order payable to ASIS-NAPS.

[^3]:    ${ }^{a}$ These parameters are defined with respect to the pseudo tetragonal unit-cell (which has previously been accepted for $\mathrm{H}-\mathrm{Ta}_{2} \mathrm{O}_{5}$ ).
    ${ }^{b}$ The form of the anisotropic thermal ellipsoid is

